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К. И. Сатпаев атындағы Қазақ ұлттық техникалық зерттеу университеті

# Х А Б А Р Л А Р Ы

## ИЗВЕСТИЯ

НАЦИОНАЛЬНОЙ АКАДЕМИИ НАУК  
РЕСПУБЛИКИ КАЗАХСТАН  
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## NEWS

OF THE ACADEMY OF SCIENCES  
OF THE REPUBLIC OF KAZAKHSTAN  
Kazakh national research technical university  
named after K. I. Satpayev

### ГЕОЛОГИЯ ЖӘНЕ ТЕХНИКАЛЫҚ ҒЫЛЫМДАР СЕРИЯСЫ

### ◆ СЕРИЯ ГЕОЛОГИИ И ТЕХНИЧЕСКИХ НАУК

### ◆ SERIES OF GEOLOGY AND TECHNICAL SCIENCES

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ЖЫЛЫНА 6 РЕТ ШЫГАДЫ  
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*NAS RK is pleased to announce that News of NAS RK. Series of geology and technical sciences scientific journal has been accepted for indexing in the Emerging Sources Citation Index, a new edition of Web of Science. Content in this index is under consideration by Clarivate Analytics to be accepted in the Science Citation Index Expanded, the Social Sciences Citation Index, and the Arts & Humanities Citation Index. The quality and depth of content Web of Science offers to researchers, authors, publishers, and institutions sets it apart from other research databases. The inclusion of News of NAS RK. Series of geology and technical sciences in the Emerging Sources Citation Index demonstrates our dedication to providing the most relevant and influential content of geology and engineering sciences to our community.*

Қазақстан Республикасы Ұлттық ғылым академиясы "ҚР ҰҒА Хабарлары. Геология және техникалық ғылымдар сериясы" ғылыми журналының Web of Science-тің жаңаланған нұсқасы Emerging Sources Citation Index-те индекстелуге қабылданғанын хабарлайды. Бұл индекстелу барысында Clarivate Analytics компаниясы журналды одан әрі the Science Citation Index Expanded, the Social Sciences Citation Index және the Arts & Humanities Citation Index-ке қабылдау мәселесін қарастыруды. Web of Science зерттеушілер, авторлар, баспашилар мен мекемелерге контент тереңдігі мен сапасын ұсынады. ҚР ҰҒА Хабарлары. Геология және техникалық ғылымдар сериясы Emerging Sources Citation Index-ке енүі біздің қоғамдастық үшін ең өзекті және беделді геология және техникалық ғылымдар бойынша контентке адалдығымызды білдіреді.

НАН РК сообщает, что научный журнал «Известия НАН РК. Серия геологии и технических наук» был принят для индексирования в Emerging Sources Citation Index, обновленной версии Web of Science. Содержание в этом индексировании находится в стадии рассмотрения компанией Clarivate Analytics для дальнейшего принятия журнала в the Science Citation Index Expanded, the Social Sciences Citation Index и the Arts & Humanities Citation Index. Web of Science предлагает качество и глубину контента для исследователей, авторов, издателей и учреждений. Включение Известия НАН РК. Серия геологии и технических наук в Emerging Sources Citation Index демонстрирует нашу приверженность к наиболее актуальному и влиятельному контенту по геологии и техническим наукам для нашего сообщества.

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## **CALCULATION AND VISUALIZATION OF A BODY MOTION IN A GRAVITATIONAL FIELD**

**Abstract.** The article presents the program for calculation and visualization of a material particle motion trajectory in a gravitational field of two motionless objects M1 and M2. The system of differential equations of the particle motion is solved using the ode45 procedure of the MATLAB system. At first the m-file under the title «f=finit2(t,x)», is created and then it is connected from a command line. Experiments with change of mass of the second motionless object are made, i.e. at M1=50 for M2=0; 0.2; 1; 2; at M1=49 for M2=0; 1; 2; at M1=47 for M2=0.5; 1.0. The movement of a point in the field of one motionless object happens along an ellipse, and introduction of other motionless object of small mass leads to perturbation of an orbit and the trajectory isn't closed. Initial parameters are introduced as global. By changing initial parameters it is possible to get various models of the particle's motion in the gravitational field. The results of this study can be used on theoretical mechanics classes of the higher school.

**Key words:** gravitational field, trajectory, perturbation, ode45 procedure.

Nowadays all educational institutions of Kazakhstan are provided with computer hardware and software, interactive boards and internet. Almost all teachers have completed language and computer courses of professional development. Hence the educational institutions have all conditions for using computer training programs and models for performing computer laboratory works. In recent years we conduct work on organization computer laboratory works on physics with use of resources of the Fizikon Company [1] and [2], developed at Al-Farabi Kazakh National University by V. V. Kashkarov and his group. Some of worksheet templates for computer laboratory works are introduced in educational process of our university and schools of the Southern Kazakhstan [3-29]. Students of the specialties 5B060400 and 5B011000-physics successfully study the discipline “Computer modeling of physical phenomena” which is the logical continuation of the disciplines “Information technologies in teaching physics” and “Use of electronic textbooks in teaching physics”. The aim of this discipline is to study and learn the program language of the MATLAB [30] system, acquaintance with its huge opportunities for the modeling and visualization of physical processes. The MATLAB system is widely applied for calculating and visualization of problems of applied mechanics which are studied by students of specialties 5B070600-Geology and exploration of mineral deposits, 5B071200-Mechanical engineering, 5B072900-Construction, 5B072400-Technological machines and the equipment, 5B071300-Transport, transport equipment and technologies, 5B070800-Oil and gas business, 5B090100-Organization of transports, movement and operation of transport.

This article is devoted to calculation and visualization of a body motion in a gravitational field using MATLAB software package.

Laboratory work “Calculation and visualization of a body motion in a gravitational field of two motionless objects”.

Aim of the work: to work out the program for calculation and visualization of a body motion in a gravitational field of two motionless objects.

Formulation of the problem: A particle of mass  $m$  moves in a gravitational field of two motionless objects with masses  $M_1$  and  $M_2$  (figure 1).

The motion of the particle with mass  $m$  is described by the following equation

$$m\ddot{\vec{R}} = -G \frac{mM_1}{|\vec{R} - \vec{r}_1|^3} (\vec{R} - \vec{r}_1) - G \frac{mM_2}{|\vec{R} - \vec{r}_2|^3} (\vec{R} - \vec{r}_2) \quad (1)$$

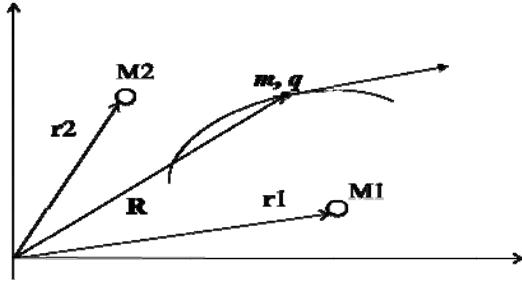


Figure 1 – The diagram of a location of the particle with mass  $m$  in gravitational field of two motionless objects with masses  $M_1$  and  $M_2$

The equation (1) is the second-order differential equation. It can be reduced to the first-order equation:

$$\begin{aligned} \dot{\vec{R}} &= \vec{V} \\ \dot{\vec{V}} &= -G \frac{M_1}{|\vec{R} - \vec{r}_1|^3} (\vec{R} - \vec{r}_1) - G \frac{M_2}{|\vec{R} - \vec{r}_2|^3} (\vec{R} - \vec{r}_2) \end{aligned} \quad (2)$$

We suppose that motion occurs on the plane and introduce the following denotations:

$$\vec{R} = (x_1, x_2), \vec{r}_1 = (c_1 x, c_1 y), \vec{r}_2 = (c_2 x, c_2 y), \vec{V} = (x_3, x_4) \quad (3)$$

Using these denotations we rewrite the equation (2) as the followings

$$\begin{aligned} \dot{x}_1 &= x_3; \quad \dot{x}_2 = x_4; \\ \dot{x}_3 &= -G \frac{M_1(x_1 - c_1 x)}{\left((x_1 - c_1 x)^2 + (x_2 - c_1 y)^2\right)^{3/2}} - \frac{M_2(x_1 - c_2 x)}{\left((x_1 - c_2 x)^2 + (x_2 - c_2 y)^2\right)^{3/2}}; \\ \dot{x}_4 &= -G \frac{M_1(x_2 - c_1 y)}{\left((x_1 - c_1 x)^2 + (x_2 - c_1 y)^2\right)^{3/2}} - \frac{M_2(x_2 - c_2 y)}{\left((x_1 - c_2 x)^2 + (x_2 - c_2 y)^2\right)^{3/2}}; \end{aligned} \quad (4)$$

Without impact on the solution of the problem, we take the value of a gravitational constant to be equal to  $G=1$  and  $M_1=50$ ,  $M_2=0$  (their values can be changed). Also we suppose that coordinates of motionless objects are  $c_1=(5,0)$ ,  $c_2=(0,10)$ . Then the system of the equations can be written as m. file under the title finit2.

Listing of the m. file

```
f=finit2(t,x)
global M1 M2 c1x c1y c2x c2y
f=[x(3);x(4);...
-M1*(x(1)-c1x)/(sqrt((x(1)-c1x)^2+(x(2)-c1y)^2))^3-...
M2*(x(1)-c2x)/(sqrt((x(1)-c2x)^2+(x(2)-c2y)^2))^3;
-M1*(x(2)-c1y)/(sqrt((x(1)-c1x)^2+(x(2)-c1y)^2))^3-...
M2*(x(2)-c2y)/(sqrt((x(1)-c2x)^2+(x(2)-c2y)^2))^3];
end
```

The program of the movement of a particle of mass  $m$  in the field of one motionless object with mass  $M_1=50$ . In the command line of MATLAB we write

```
>> global M1 M2 c1x c1y c2x c2y
>> M1=50; M2=0; c1x=5; c1y=0; c2x=0; c2y=10; % input of parameters
>> x0=0; y0=0; vx0=0; vy0=4.3; T1=4000; % input of parameter
>> [t,h]=ode45(@finit2,[0,T1],[x0,y0,vx0,vy0]); % solution of the differential equation
>> x=h(:,1); y=h(:,2); x1=c1x; y1=c1y; x2=c2x; y2=c2y;
>> plot(x,y) % drawing the motion trajectory
>> grid on% drawing the coordinate grid
>> hold on% drawing the next element
% drawing the location of motionless objects
>> plot(x1,y1,'r+',x2,y2,'r*','MarkerSize',15);
>> plot(x1,y1,'ro',x2,y2,'ro','MarkerSize',15);
>> gtext('M1=50') % input of the notation in the figure
>> gtext('M2=0') % input of the notation in the figure
```

The result is presented in the figure 2.

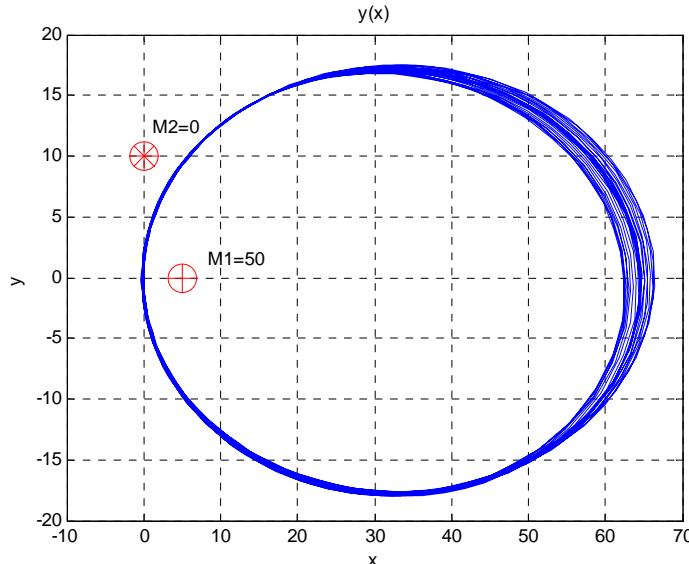


Figure 2 – The trajectory of a particle motion in a gravitational field of one motionless object with mass  $M_1$

It is known that the particle in a gravitational field of one motionless object with a certain mass moves along an ellipse or a circle. In the figure 2 the line trajectory is indistinct. This is due to insufficient accuracy of the calculation. By default the accuracy of calculation of the ode45 procedure is 1e-6 which isn't enough for the considered problem. Therefore, in the ode45 procedure the calculation accuracy is taken to be 1e-9.

```
>> global M1 M2 c1x c1y c2x c2y
>> M1=50; M2=0; c1x=5; c1y=0; c2x=0; c2y=10; % input of parameters
>> x0=0; y0=0; vx0=0; vy0=4.3; T1=4000;
>> tol=1e-9;
>> [t,h]=ode45(@finit2,[0,T1],[x0,y0,vx0,vy0],odeset('RelTol',tol));
>> x=h(:,1); y=h(:,2); x1=c1x; y1=c1y; x2=c2x; y2=c2y;
>> plot(x,y) % drawing the trajectory of the motion
>> grid on
>> hold on% drawing the next element
% drawing the location of motionless objects
>> plot(x1,y1,'r+',x2,y2,'r*','MarkerSize',15);
>> plot(x1,y1,'ro',x2,y2,'ro','MarkerSize',15);
```

```
>> gtext('M1=50') % input of the notation in the figure
>> gtext('M2=0') % input of the notation in the figure
The result is presented in the figure 3.
```

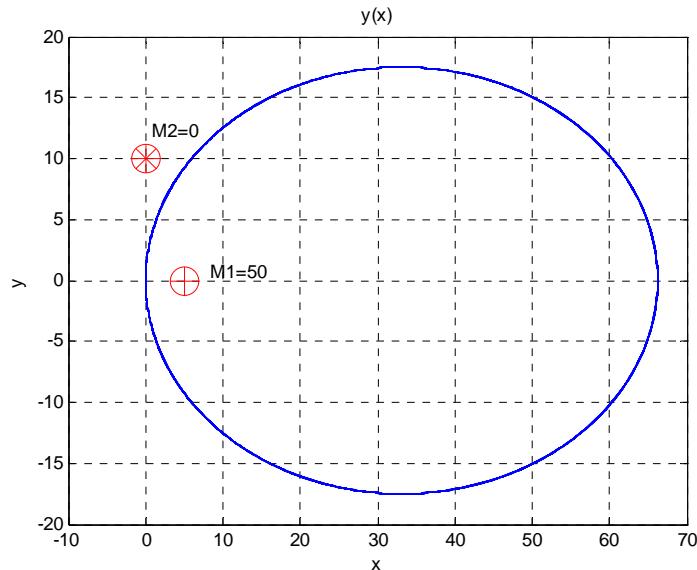


Figure 3 – The trajectory of a particle motion in a gravitational field of one motionless object with mass M1

Now we have got the perfect picture of the trajectory.

The program of the movement of a particle of mass  $m$  in the field of two motionless objects with masses  $M1=50$  and  $M2=0.2$ .

```
>> M1=50; M2=0.2; c1x=5; c1y=0; c2x=0; c2y=10; % input of parameters
>> x0=0; y0=0; vx0=0; vy0=4.3; T1=1000; % input of parameters
>> [t,h]=ode45(@finit2,[0,T1],[x0,y0,vx0,vy0]); % solution of the differential equation
>> x=h(:,1); y=h(:,2); x1=c1x; y1=c1y; x2=c2x; y2=c2y;
>> plot(x,y); % drawing the motion trajectory
>> gtext('M2=0.2') % input of the notation in the figure
>> gtext('M1=50') % input of the notation in the figure
```

The result is presented in the figure 4.

Figure 4 shows that introduction of the second motionless object with a small mass of  $M2=0.2$  leads to disturbance of an orbit and the orbit isn't closed.

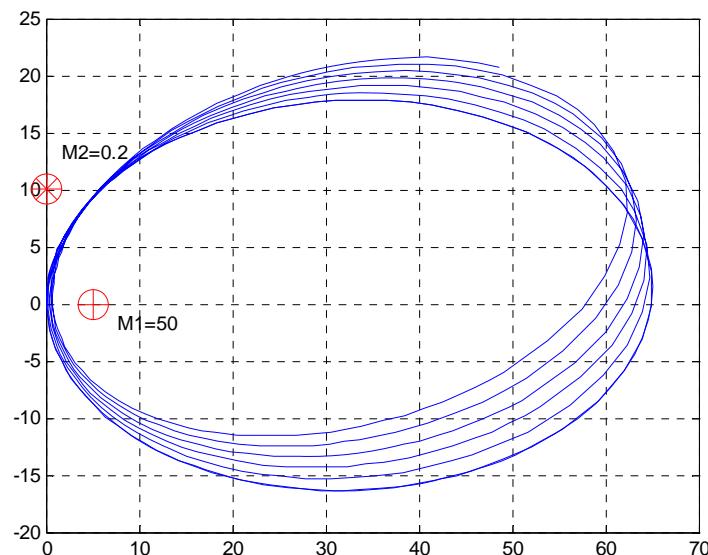


Figure 4 – The trajectory of a particle motion in a gravitational field of two motionless objects with masses M1=50 and M2=0.2

The program of the movement of a particle of mass  $m$  in the field of two motionless objects with masses  $M_1=50$  and  $M_2=1$ .

```
>> global M1 M2 c1x c1y c2x c2y
>> M1=50; M2=1; c1x=5; c1y=0; c2x=0; c2y=10; % input of parameters
>> x0=0; y0=0; vx0=0; vy0=4.3; T1=1000; % input of parameters
>> [t,h]=ode45(@finit2,[0,T1],[x0,y0,vx0,vy0]); % solution of the differential equation
>> x=h(:,1); y=h(:,2); x1=c1x; y1=c1y; x2=c2x; y2=c2y;
>> plot(x,y); % drawing the motion trajectory
>> grid on% drawing the coordinate grid
>> hold on% drawing the next element
>> % drawing the location of motionless objects
>> plot(x1,y1,'r+',x2,y2,'r*','MarkerSize',15);
>> plot(x1,y1,'ro',x2,y2,'ro','MarkerSize',15);
>> gtext('M1=50') % input of the notation in the figure
>> gtext('M2=1') % input of the notation in the figure
```

The result is presented in the figure 5.

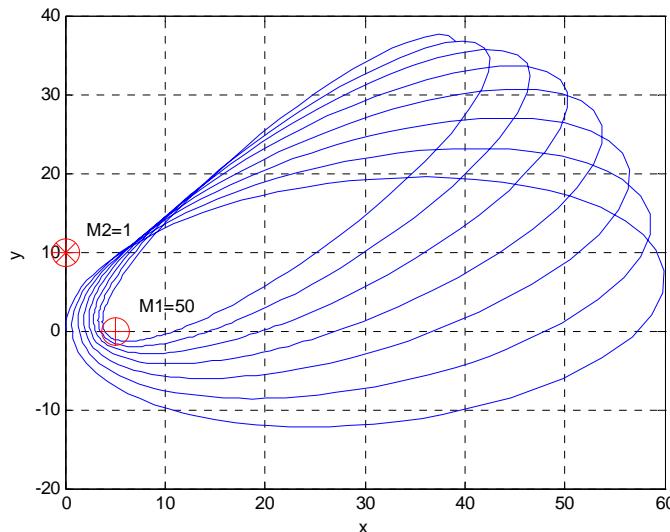


Figure 5 – The trajectory of a particle motion in a gravitational field of two motionless objects with masses  $M_1=50$  and  $M_2=1$

Figure 5 shows that the increase in mass of the second motionless object leads to a greater disturbance of the orbit.

The program of the movement of a particle of mass  $m$  in the field of two motionless objects with masses  $M_1=50$  and  $M_2=2$ .

```
>> global M1 M2 c1x c1y c2x c2y
>> M1=50; M2=2; c1x=5; c1y=0; c2x=0; c2y=10; % input of parameters
>> x0=0; y0=0; vx0=0; vy0=4.3; T1=1000; % input of parameters
>> [t,h]=ode45(@finit2,[0,T1],[x0,y0,vx0,vy0]); % solution of the differential equation
>> x=h(:,1); y=h(:,2); x1=c1x; y1=c1y; x2=c2x; y2=c2y;
>> plot(x,y); % drawing the motion trajectory
>> grid on% drawing the coordinate grid
>> hold on% drawing the next element
>> % drawing the location of motionless objects
>> plot(x1,y1,'r+',x2,y2,'r*','MarkerSize',15);
>> plot(x1,y1,'ro',x2,y2,'ro','MarkerSize',15);
>> gtext('M1=50') % input of the notation in the figure
>> gtext('M2=2') % input of the notation in the figure
```

The result is presented in the figure 6.

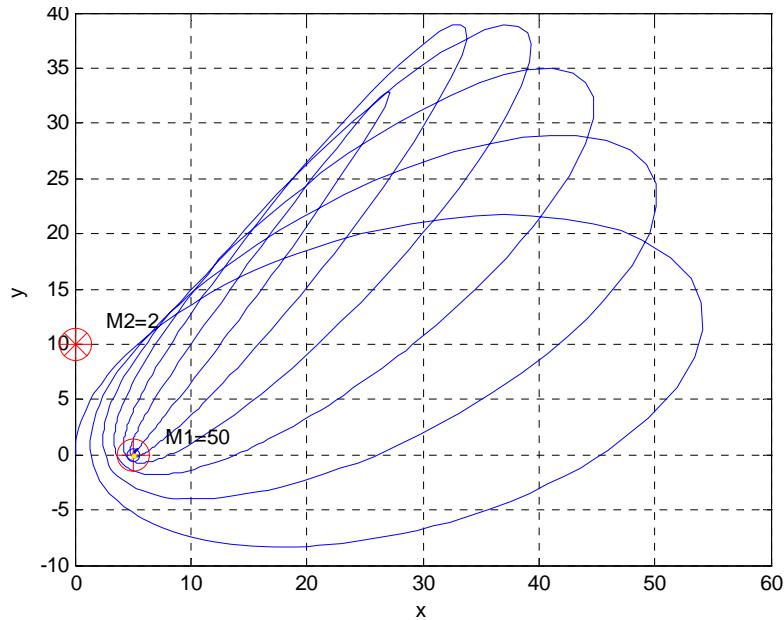


Figure 6 – The trajectory of a particle motion in a gravitational field of two motionless objects with masses  $M_1=50$  and  $M_2=2$

The program of the movement of a particle of mass  $m$  in the field of two motionless objects with masses  $M_1=49$  and  $M_2=0$ .

```
>> global M1 M2 c1x c1y c2x c2y
>> M1=49; M2=0; c1x=5; c1y=0; c2x=0; c2y=10; % input of parameters
>> x0=0; y0=0; vx0=0; vy0=4.3; T1=300; % input of parameters
>> [t,h]=ode45(@finit2,[0,T1],[x0,y0,vx0,vy0]); % solution of the differential equation
>> x=h(:,1); y=h(:,2); x1=c1x; y1=c1y; x2=c2x; y2=c2y;
>> plot(x,y); % drawing the motion trajectory
>> grid on% drawing the coordinate grid
>> hold on% drawing the next element
% drawing the location of motionless objects
>> plot(x1,y1,'r+',x2,y2,'r*','MarkerSize',15);
>> plot(x1,y1,'ro',x2,y2,'ro','MarkerSize',15);
>> gtext('M1=49') % input of the notation in the figure
>> gtext('M2=0') % input of the notation in the figure
```

The result is presented in the figure 7.

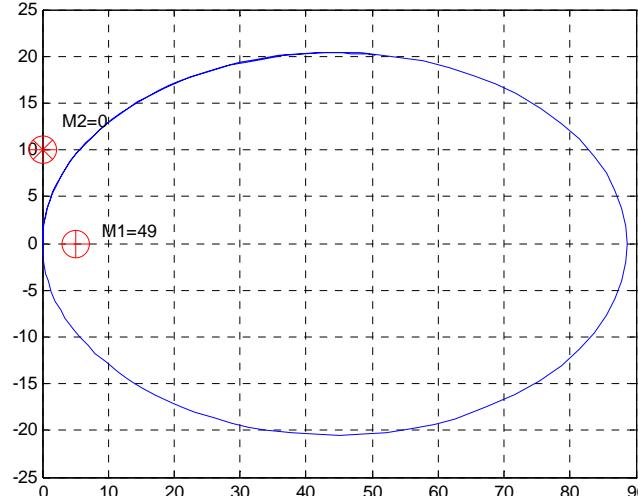


Figure 7 – The trajectory of a particle motion in a gravitational field of two motionless objects with masses  $M_1=49$  and  $M_2=0$

The program of the movement of a particle of mass  $m$  in the field of two motionless objects with masses  $M1=49$  and  $M2=1$ .

```
>> global M1 M2 c1x c1y c2x c2y
>> M1=49; M2=1; c1x=5; c1y=0; c2x=0; c2y=10; % input of parameters
>> x0=0; y0=0; vx0=0; vy0=4.3; T1=1000; % input of parameters
>> [t,h]=ode45(@finit2,[0,T1],[x0,y0,vx0,vy0]); % solution of the differential equation
>> x=h(:,1); y=h(:,2); x1=c1x; y1=c1y; x2=c2x; y2=c2y;
>> plot(x,y); % drawing the motion trajectory
>> grid on% drawing the coordinate grid
>> hold on% drawing the next element
>> % drawing the location of motionless objects
>> plot(x1,y1,'r+',x2,y2,'r*','MarkerSize',15);
>> plot(x1,y1,'ro',x2,y2,'ro','MarkerSize',15);
>> gtext('M1=49') % input of the notation in the figure
>> gtext('M2=1') % input of the notation in the figure
```

The result is presented in the figure 8.

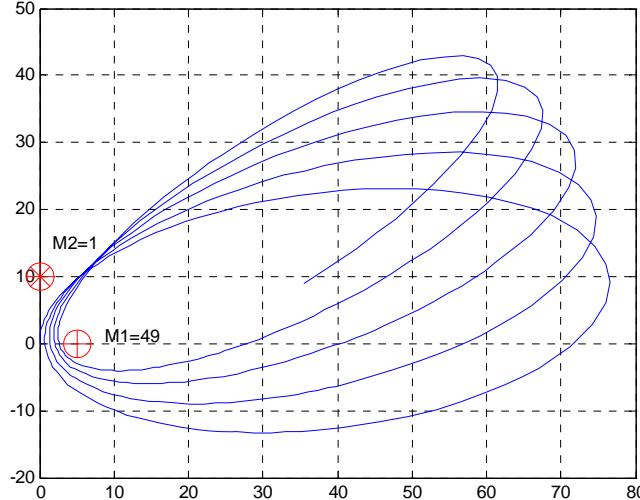


Figure 8 – The trajectory of a particle motion in a gravitational field of two motionless objects with masses  $M1=49$  and  $M2=1$

The program of the movement of a particle of mass  $m$  in the field of two motionless objects with masses  $M1=49$  and  $M2=2$ .

```
>> global M1 M2 c1x c1y c2x c2y
>> M1=49; M2=2; c1x=5; c1y=0; c2x=0; c2y=10; % input of parameters
>> x0=0; y0=0; vx0=0; vy0=4.3; T1=1000; % input of parameters
>> [t,h]=ode45(@finit2,[0,T1],[x0,y0,vx0,vy0]); % solution of the differential equation
>> x=h(:,1); y=h(:,2); x1=c1x; y1=c1y; x2=c2x; y2=c2y;
>> plot(x,y); % drawing the motion trajectory
>> grid on% drawing the coordinate grid
>> hold on% drawing the next element
% drawing the location of motionless objects
>> plot(x1,y1,'r+',x2,y2,'r*','MarkerSize',15);
>> plot(x1,y1,'ro',x2,y2,'ro','MarkerSize',15);
>> gtext('M1=49') % input of the notation in the figure
>> gtext('M2=2') % input of the notation in the figure
```

The result is presented in the figure 9.

The program of the movement of a particle of mass  $m$  in the field of two motionless objects with masses  $M1=47$  and  $M2=0.5$ .

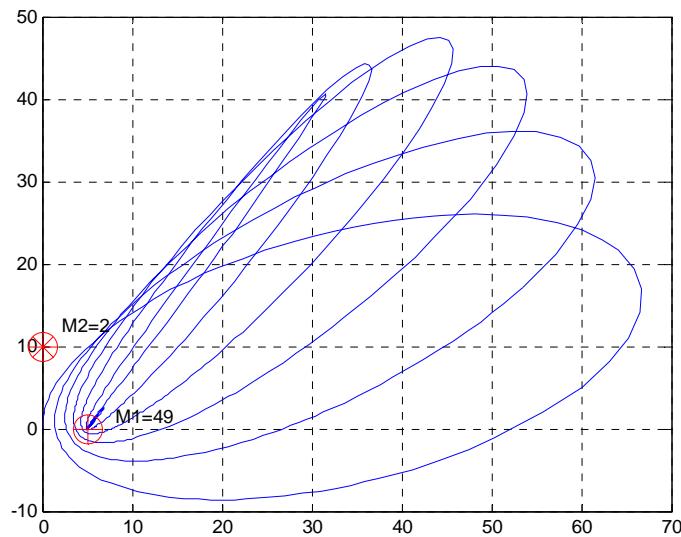


Figure 9 – The trajectory of a particle motion in a gravitational field of two motionless objects with masses  $M_1=49$  and  $M_2=2$

```
>> global M1 M2 c1x c1y c2x c2y;
>> M1=47; M2=0.5; c1x=5; c1y=0; c2x=0; c2y=10; % input of parameters
>> x0=0; y0=0; vx0=0; vy0=4.3; T1=4000; % input of parameters
>> [t,h]=ode45(@finit2,[0,T1],[x0,y0,vx0,vy0]); % solution of the differential equation
>> x=h(:,1); y=h(:,2); x1=c1x; y1=c1y; x2=c2x; y2=c2y;
>> plot(x,y); % drawing the motion trajectory
>> grid on% drawing the coordinate grid
>> hold on% drawing the next element
% drawing the location of motionless objects
>> plot(x1,y1,'r+',x2,y2,'r*','MarkerSize',15);
>> plot(x1,y1,'ro',x2,y2,'ro','MarkerSize',15);
>> gtext('M1=47') % input of the notation in the figure
>> gtext('M2=0.5') % input of the notation in the figure
The result is presented in the figure 10.
```

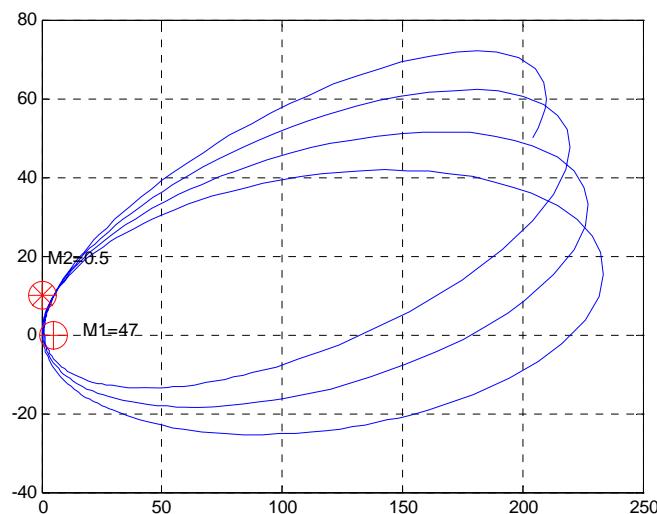


Figure 10 – The trajectory of a particle motion in a gravitational field of two motionless objects with masses  $M_1=47$  and  $M_2=0.5$

The program of the movement of a particle of mass  $m$  in the field of two motionless objects with masses  $M_1=47$  and  $M_2=1$ .

```

>> T1=4000; M1=47; M2=1;
>> [t,h]=ode45(@finit2,[0,T1],[x0,y0,vx0,vy0]); % solution of the differential equation
>> x=h(:,1); y=h(:,2); x1=c1x; y1=c1y; x2=c2x; y2=c2y;
>> plot(x,y) % drawing the motion trajectory
>> grid on% drawing the coordinate grid
>> hold on% drawing the next element
% drawing the location of motionless objects
>> plot(x1,y1,'r+',x2,y2,'r*','MarkerSize',15);
>> plot(x1,y1,'ro',x2,y2,'ro','MarkerSize',15);
>> gtext('M1=47') % input of the notation in the figure
>> gtext('M2=1') % input of the notation in the figure
The result is presented in the figure 11.

```

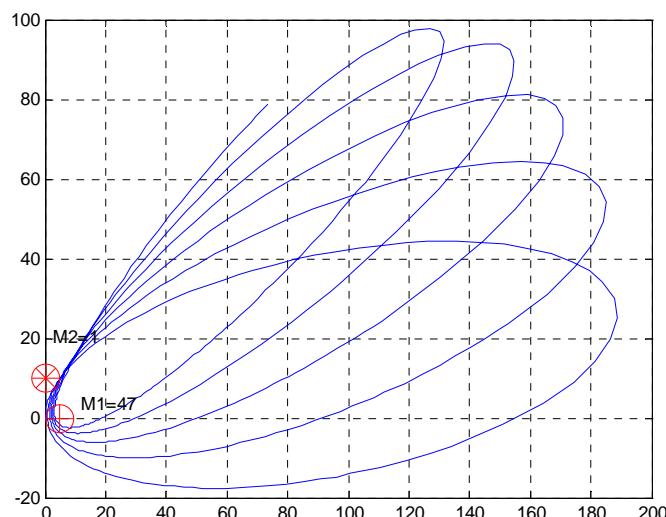


Figure 11 – The trajectory of a particle motion in a gravitational field of two motionless objects with masses  $M_1=47$  and  $M_2=1$

**Conclusion.** The program allows performing modeling at various initial parameters: for example at  $M_1=50$  and  $M_2=0$ ;  $0.2$ ;  $1$ ;  $2$ ; at  $M_1=49$  and  $M_2=0$ ;  $1$ ;  $2$ ; at  $M_1=47$  and  $M_2=0.5$ ;  $1.0$ . Students are suggested to simulate independently for other various initial parameters by changing calculation accuracy using the command “odeset(‘RelTol’, tol)”.

The use of the MATLAB language for simulation of the material particle motion in the gravitational field of two motionless objects with different masses helps greatly in study of the gravitational field influence on the particle’s motion.

The movement of the particle in the field of one motionless object happens along an ellipse, and introduction of other motionless object of small mass leads to perturbation of an orbit and the trajectory isn’t closed.

#### REFERENCES

- [1] CD of the open JSC "Phizicon". «The open hysics1.1». 2001.
- [2] <http://elektronika.newmail.ru>
- [3] Kabylbekov K.A., Abdurakhmanova Kh.K., Abekova Zh.A., Abdraimov R.T., Ualikhanova B.S. Calculation and visualization of a system- an electron in a deep square potential well, with use of the software package of MATLAB. Proceeding of the III International Scientific and Practical Conference «Topical researches of the World Science» (June 28, 2017, Dubai, UAE). July 2017. Vol. 1, N (23). P. 7-13.
- [4] Kabylbekov K., Saidullaeva N., Spabekova R., Omashova G., Tagaev N., Bitemirova A., Berdieva M. Model of a blank form for computer laboratory work on research of the speed selector // Journal of Theoretical and Applied Information Technology 15th July 2017. Vol. 95, N 13. P. 2999-3009. JATIT & LLS. Indexada en Scopus.
- [5] Kabylbekov K., Omashova G., Spabekova R., Saidullaeva N., Saidakhmetuv P., Junusbtkova S Management and organization of computer laboratory work in physics education // Espacios. Vol. 38, N 45. Año 2017. Pág. 35. Indexada en Scopus, Google Schollar.

- [6] Kabylbekov K.A., Saidakhmetov P. A., Arysbaeva A.S. Worksheet template for organization the independent performance of computer laboratory works // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2013. N 6. P. 82-89.
- [7] Kabylbekov K.A., Saidahmetov P. A., Baidullaeva L.E., Abduraimov R. A technique of use of computer models for photo-effect and Compton effect studying, worksheet template for organization the performance of computer laboratory works // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2013. N 6. P. 114-121.
- [8] Kabylbekov K.A., Saidahmetov P.A. Turganova T.K, Nurullaev M. A, Baidullaeva L.E. Model of a lesson on converging and diverging lenses // Proceedings of NAN RK. Series physical-mat. Almaty, 2014, N 2. P. 286-294.
- [9] Kabylbekov K.A., Ashirbaev H.A., Saidahmetov P.A., Rustemova K.Zh., Baidullaeva L.E. Worksheet template for organization the performance of computer laboratory work on study the diffraction of light // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics, Almaty, 2015. N 1(299). P. 71-77.
- [10] Kabylbekov K.A., Ashirbaev H.A., Takibaeva G.A., Saparbaeva E.M., Baidullaeva L.E., Adineeva Sh.I. Worksheet template for organization the performance of computer laboratory work on study the motion of charged particles in a magnetic field // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2015. N 1(299). P. 80-87.
- [11] Kabylbekov K.A., Ashirbaev H.A., Saidakhmetov P.A., Baigulova Z.A., Baidullaeva L.E. Worksheet template for organization the performance of computer laboratory work on study the Newton's rings // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2015. N 1(299). P. 14-20.
- [12] Kabylbekov K.A., Ashirbaev H.A., Sabalakhova A.P., Dzhumagalieva A.I. Worksheet template for organization the performance of computer laboratory work on study the phenomenon of light interference // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2015. N 3(301). P. 131-136.
- [13] Kabylbekov K.A., Ashirbaev H.A., Sabalakhova A.P., Dzhumagalieva A.I. Worksheet template for organization the performance of computer laboratory work on study the Doppler-effect // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2015. N 3(301). P. 155-160.
- [14] Kabylbekov K.A., Ashirbaev H.A., Arysbaeva A.S., Dzhumagalieva A.I. Worksheet template for organization the performance of computer laboratory work on study physical phenomena // Modern high technologies. M., 2015. N 4. P. 40-43.
- [15] Kabylbekov K. A., Saidakhmetov P. A., Ashirbaev Kh. A., Omashova G. Sh., Berdalieva J. Worksheet template for organization the performance of computer laboratory work on study electromagnetic oscillations // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics And Mathematics. Almaty, 2016. N 1(305). P. 111-116.
- [16] Kabylbekov K.A., Saidakhmetov P.A., Omashova G.Sh., Berdalieva J., Dzhumagalieva A.I. Worksheet template for organization the performance of computer laboratory work on study the interaction between two infinitely long parallel current-carrying conductors // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2016. N 1(305). P. 135-140.
- [17] Kabylbekov K.A., Saidakhmetov P.A., Omashova G.Sh., Sutibaeva D.I., Kozybakova G.N. Worksheet template for organization the performance of computer laboratory work on study isobaric process // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2016. N 2. P. 92-97.
- [18] Kabylbekov K.A., Omashova G.Sh., Saidakhmetov P.A., Nurullaev M.A., Artygalin N.A. Worksheet template for organization the performance of computer laboratory work on study the Carnot cycle // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2016. N 2. P. 98-103.
- [19] Kabylbekov K.A., Saidakhmetov P.A., Ashirbaev H.A., Abdubaeva Ph.I., Doskanova A.E. Study of the work done by gas on computer model // The Herald of NAN PK. 2016. N 2. P. 83-88.
- [20] Kabylbekov K.A., Saidakhmetov P.A., Omashova G.Sh., Serikbaeva G.S., Suyerkulova Zh.N. Worksheet template for organization the performance of computer laboratory work on study simple harmonic motions // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2016. N 2. P. 84-91.
- [21] Kabylbekov K.A. Madjarov N.T., Saidakhmetov P.A. An Independent design of research assignments for computer laboratory work on thermodynamics // Proceedings of the IX International scientific-methodical conference "Teaching natural Sciences (biology, physics, chemistry), mathematics and computer science". Tomsk, 2016. P. 93-99.
- [22] Kabylbekov K.A., Saidakhmetov P.A., Omashova G.Sh. Organization of computer laboratory work on study the inductor reactance in an ac circuit // Proceedings of NAN RK. Almaty, 2017. N 1. P. 77-82.
- [23] Kabylbekov K.A., Saidakhmetov P.A., Omashova G.Sh., Ashirbaev H.A., Abekova J.A. Organization of computer laboratory works on study of the isotherms of a real gas // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2017. N 1. P. 77-83.
- [24] Kabylbekov K.A., Saidakhmetov P.A., Omashova G.Sh. Organization of computer laboratory works on study of the phenomenon of beats // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2017. N 2. P. 104-110.
- [25] Kabylbekov K.A., Omashova G.Sh., Spabekova R.S., Saidakhmetov P.A., Serikbaeva G., Arysbaeva A.S. Worksheet template for organization the performance of computer laboratory work on study the isothermal process // Herald of the National Academy of Sciences of Kazakhstan. Almaty, 2017. N 3. P. 19-207.
- [26] Kabylbekov K.A., Omashova G.Sh., Spabekova R.S., Saidakhmetov P.A., Abdrikhanova Kh.K., Arysbaeva A.S. Independent design of assignment for performance of a computer lab on study isochoric process // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2017. N 3. P. 127-134.
- [27] Kabylbekov K.A., Omashova G.Sh., Spabekova R.S., Saidakhmetov P.A., Serikbaeva G.S., Aktureeva G. Organization of computer laboratory works on study the turn-on and turn-off current of the power supply by using MATLAB software package

// Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2017. N 3. P. 139-146.

[28] Kabylbekov K.A., Omashova G.Sh., Spabekova R.S., Saidakhmetov P.A., Serikbaeva G.S., Aktureeva G. Organization of computer labs for the study the velocity and height distribution of molecules from the Earth's surface by using MATLAB software package // Herald of RK NAS. Almaty, 2017. N 3. P. 111-119.

[29] Kabylbekov K.A., Ashirbayev H.A., Abdrikhmanova Kh.K., Dzhumagalieva A.I., Kydyrbekova J.B. Organization of laboratory work on study the electric and magnetic fields by using MATLAB software package // Proceedings of the National Academy of Sciences of the Republic of Kazakhstan. Series of Physics and Mathematics. Almaty, 2017. N 3(313). P. 206-212.

[30] Porsev S.V. Computer simulation of physical processes in the package MATLAB. M.: Hot Line-Telecom, 2003. 592 p.

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### **ДЕҢЕНИҚ ГРАВИТАЦИЯЛЫҚ ӨРІСТЕ ҚОЗГАЛЫСЫН ЕСЕПТЕУ МЕН БЕЙНЕЛЕУ**

**Аннотация.** Екі тыныштықтағы M1 және M2 объектілердің гравитациялық өрісінде материалың нүктенің траекториясын есептеу мен бейнелеу ұсынылған. Предлагается программа расчета и визуализации. Қозгалыстың дифференциалдық тендеулер жүйесі MATLAB жүйесінде ode45 процедурасымен шешіледі. Ол үшін алдын-ала «f=finit2(t,x)» деп атаптын т-файл жазылады және ол MATLAB тың командалық строкасынан қосылады. Тыныштықтағы бірінші объектінің массасын өзгертпей M1=50, тыныштықтағы екінші объектінің массасын M2=0; 0.2; 1; 2 шамаларында өзгертіп эксперименттер жүргізілген;

Сонымен қатар M1=49, M2=0, 1, 2; M1=47, M1=0.5, 1.0 шамалар бойынша эксперименттер қайталанған. Тыныштықтағы бір объектінің өрісінде материалың нүктенің қозгалысы эллипс бойында, ал екінші объект қосылғанда нүктенің траекториясы шамалы өзгереді де траектория тұйықталмайды. Бастапқы параметрлер глобалды деп жарияланған. Бастапқы параметрлерін өзгерту арқылы материалдық нүктенің гравитациялық өрістегі қозгалысының әр түрлі моделін алуға болады.

Зерттеу нәтижелері жоғары оқу орындарындағы теориялық механика дәрістерінде қолдануға болады.

**Түйін сөздер:** гравитациялық өріс, траектория, өзгерту, ode45 процедурасы.

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### **РАСЧЕТ И ВИЗУАЛИЗАЦИЯ ДВИЖЕНИЯ ТЕЛА В ГРАВИТАЦИОННОМ ПОЛЕ**

**Аннотация.** В статье приводится расчет и визуализация траектории движения материальной точки в гравитационном поле двух неподвижных объектов M1 и M2. Решение системы дифференциальных уравнений движения проводится процедурой ode45 системы MATLAB. Сначала создается т-файл под названием «f=finit2(t,x)», который подключается с командной строки. Далее проводится моделирование с изменением массы второго неподвижного объекта при постоянной массе первого объекта: M2=0; 1; 2 при M1=50; M2=0, 1, 2 при M1=49; M1=0.5 и 1.0 при M1=47. Движение точки в поле одного неподвижного объекта происходит по эллипсу, а введение другого неподвижного объекта малой массы приводит к возмущению орбиты и траектория незамкнута. Исходные параметры объявлены как глобальные. Меняя исходные параметры можно получить разные модели движения материальной точки в гравитационном поле.

Результаты исследования могут быть использованы на занятиях по теоретической механике в высших учебных заведениях.

**Ключевые слова:** гравитационное поле, траектория, возмущение, процедура ode45.

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