

ISSN 2518-170X (Online),  
ISSN 2224-5278 (Print)

ҚАЗАҚСТАН РЕСПУБЛИКАСЫ  
ҰЛТТЫҚ ҒЫЛЫМ АКАДЕМИЯСЫНЫҢ  
Қ. И. Сәтпаев атындағы Қазақ ұлттық техникалық зерттеу университеті

# Х А Б А Р Л А Р Ы

---

---

## ИЗВЕСТИЯ

НАЦИОНАЛЬНОЙ АКАДЕМИИ НАУК  
РЕСПУБЛИКИ КАЗАХСТАН  
Қазақстан Республикасының Ғылым Академиясының  
Қ. И. Сәтпаев атындағы Қазақ ұлттық техникалық зерттеу университеті

## NEWS

OF THE ACADEMY OF SCIENCES  
OF THE REPUBLIC OF KAZAKHSTAN  
Kazakh national research technical university  
named after K. I. Satpayev

**SERIES  
OF GEOLOGY AND TECHNICAL SCIENCES**

**1 (433)**

**JANUARY – FEBRUARY 2019**

THE JOURNAL WAS FOUNDED IN 1940

PUBLISHED 6 TIMES A YEAR

ALMATY, NAS RK

---

*NAS RK is pleased to announce that News of NAS RK. Series of geology and technical sciences scientific journal has been accepted for indexing in the Emerging Sources Citation Index, a new edition of Web of Science. Content in this index is under consideration by Clarivate Analytics to be accepted in the Science Citation Index Expanded, the Social Sciences Citation Index, and the Arts & Humanities Citation Index. The quality and depth of content Web of Science offers to researchers, authors, publishers, and institutions sets it apart from other research databases. The inclusion of News of NAS RK. Series of geology and technical sciences in the Emerging Sources Citation Index demonstrates our dedication to providing the most relevant and influential content of geology and engineering sciences to our community.*

*Қазақстан Республикасы Ұлттық ғылым академиясы "ҚР ҰҒА Хабарлары. Геология және техникалық ғылымдар сериясы" ғылыми журналының Web of Science-тің жаңаланған нұсқасы Emerging Sources Citation Index-те индекстелуге қабылданғанын хабарлайды. Бұл индекстелу барысында Clarivate Analytics компаниясы журналды одан әрі the Science Citation Index Expanded, the Social Sciences Citation Index және the Arts & Humanities Citation Index-ке қабылдау мәселесін қарастыруда. Web of Science зерттеушілер, авторлар, баспашылар мен мекемелерге контент тереңдігі мен сапасын ұсынады. ҚР ҰҒА Хабарлары. Геология және техникалық ғылымдар сериясы Emerging Sources Citation Index-ке енуі біздің қоғамдастық үшін ең өзекті және беделді геология және техникалық ғылымдар бойынша контентке адалдығымызды білдіреді.*

*НАН РК сообщает, что научный журнал «Известия НАН РК. Серия геологии и технических наук» был принят для индексирования в Emerging Sources Citation Index, обновленной версии Web of Science. Содержание в этом индексировании находится в стадии рассмотрения компанией Clarivate Analytics для дальнейшего принятия журнала в the Science Citation Index Expanded, the Social Sciences Citation Index и the Arts & Humanities Citation Index. Web of Science предлагает качество и глубину контента для исследователей, авторов, издателей и учреждений. Включение Известия НАН РК. Серия геологии и технических наук в Emerging Sources Citation Index демонстрирует нашу приверженность к наиболее актуальному и влиятельному контенту по геологии и техническим наукам для нашего сообщества.*

Б а с р е д а к т о р ы  
э. ғ. д., профессор, ҚР ҰҒА академигі

**И.К. Бейсембетов**

Бас редакторының орынбасары

**Жолтаев Г.Ж.** проф., геол.-мин. ғ. докторы

Р е д а к ц и я а л қ а с ы:

**Абаканов Т.Д.** проф. (Қазақстан)  
**Абишева З.С.** проф., академик (Қазақстан)  
**Агабеков В.Е.** академик (Беларусь)  
**Алиев Т.** проф., академик (Әзірбайжан)  
**Бакиров А.Б.** проф., (Қырғыстан)  
**Беспәев Х.А.** проф. (Қазақстан)  
**Бишимбаев В.К.** проф., академик (Қазақстан)  
**Буктуков Н.С.** проф., академик (Қазақстан)  
**Булат А.Ф.** проф., академик (Украина)  
**Ганиев И.Н.** проф., академик (Тәжікстан)  
**Грэвис Р.М.** проф. (АҚШ)  
**Ерғалиев Г.К.** проф., академик (Қазақстан)  
**Жуков Н.М.** проф. (Қазақстан)  
**Қожахметов С.М.** проф., академик (Қазақстан)  
**Конторович А.Э.** проф., академик (Ресей)  
**Курскеев А.К.** проф., академик (Қазақстан)  
**Курчавов А.М.** проф., (Ресей)  
**Медеу А.Р.** проф., академик (Қазақстан)  
**Мұхамеджанов М.А.** проф., корр.-мүшесі (Қазақстан)  
**Нигматова С.А.** проф. (Қазақстан)  
**Оздоев С.М.** проф., академик (Қазақстан)  
**Постолатий В.** проф., академик (Молдова)  
**Ракишев Б.Р.** проф., академик (Қазақстан)  
**Сейтов Н.С.** проф., корр.-мүшесі (Қазақстан)  
**Сейтмуратова Э.Ю.** проф., корр.-мүшесі (Қазақстан)  
**Степанец В.Г.** проф., (Германия)  
**Хамфери Дж.Д.** проф. (АҚШ)  
**Штейнер М.** проф. (Германия)

«ҚР ҰҒА Хабарлары. Геология мен техникалық ғылымдар сериясы».

**ISSN 2518-170X (Online),**

**ISSN 2224-5278 (Print)**

Меншіктенуші: «Қазақстан Республикасының Ұлттық ғылым академиясы» РҚБ (Алматы қ.).

Қазақстан республикасының Мәдениет пен ақпарат министрлігінің Ақпарат және мұрағат комитетінде  
30.04.2010 ж. берілген №10892-Ж мерзімдік басылым тіркеуіне қойылу туралы куәлік.

Мерзімділігі: жылына 6 рет.

Тиражы: 300 дана.

Редакцияның мекенжайы: 050010, Алматы қ., Шевченко көш., 28, 219 бөл., 220, тел.: 272-13-19, 272-13-18,  
<http://www.geolog-technical.kz/index.php/en/>

---

© Қазақстан Республикасының Ұлттық ғылым академиясы, 2019

Редакцияның Қазақстан, 050010, Алматы қ., Қабанбай батыра көш., 69а.

мекенжайы: Қ. И. Сәтбаев атындағы геология ғылымдар институты, 334 бөлме. Тел.: 291-59-38.

Типографияның мекенжайы: «Аруна» ЖК, Алматы қ., Муратбаева көш., 75.

Г л а в н ы й р е д а к т о р  
д. э. н., профессор, академик НАН РК

**И. К. Бейсембетов**

Заместитель главного редактора

**Жолтаев Г.Ж.** проф., доктор геол.-мин. наук

Р е д а к ц и о н н а я к о л л е г и я:

**Абаканов Т.Д.** проф. (Казахстан)  
**Абишева З.С.** проф., академик (Казахстан)  
**Агабеков В.Е.** академик (Беларусь)  
**Алиев Т.** проф., академик (Азербайджан)  
**Бакиров А.Б.** проф., (Кыргызстан)  
**Беспаяев Х.А.** проф. (Казахстан)  
**Бишимбаев В.К.** проф., академик (Казахстан)  
**Буктуков Н.С.** проф., академик (Казахстан)  
**Булат А.Ф.** проф., академик (Украина)  
**Ганиев И.Н.** проф., академик (Таджикистан)  
**Грэвис Р.М.** проф. (США)  
**Ергалиев Г.К.** проф., академик (Казахстан)  
**Жуков Н.М.** проф. (Казахстан)  
**Кожаметов С.М.** проф., академик (Казахстан)  
**Конторович А.Э.** проф., академик (Россия)  
**Курскеев А.К.** проф., академик (Казахстан)  
**Курчавов А.М.** проф., (Россия)  
**Медеу А.Р.** проф., академик (Казахстан)  
**Мухамеджанов М.А.** проф., чл.-корр. (Казахстан)  
**Нигматова С.А.** проф. (Казахстан)  
**Оздоев С.М.** проф., академик (Казахстан)  
**Постолатий В.** проф., академик (Молдова)  
**Ракишев Б.Р.** проф., академик (Казахстан)  
**Сейтов Н.С.** проф., чл.-корр. (Казахстан)  
**Сейтмуратова Э.Ю.** проф., чл.-корр. (Казахстан)  
**Степанец В.Г.** проф., (Германия)  
**Хамфери Дж.Д.** проф. (США)  
**Штейнер М.** проф. (Германия)

«Известия НАН РК. Серия геологии и технических наук».

**ISSN 2518-170X (Online),**

**ISSN 2224-5278 (Print)**

Собственник: Республиканское общественное объединение «Национальная академия наук Республики Казахстан (г. Алматы)

Свидетельство о постановке на учет периодического печатного издания в Комитете информации и архивов Министерства культуры и информации Республики Казахстан №10892-Ж, выданное 30.04.2010 г.

Периодичность: 6 раз в год

Тираж: 300 экземпляров

Адрес редакции: 050010, г. Алматы, ул. Шевченко, 28, ком. 219, 220, тел.: 272-13-19, 272-13-18,  
<http://nauka-nanrk.kz/geology-technical.kz>

---

© Национальная академия наук Республики Казахстан, 2019

Адрес редакции: Казахстан, 050010, г. Алматы, ул. Кабанбай батыра, 69а.

Институт геологических наук им. К. И. Сатпаева, комната 334. Тел.: 291-59-38.

Адрес типографии: ИП «Аруна», г. Алматы, ул. Муратбаева, 75

E d i t o r i n c h i e f

doctor of Economics, professor, academician of NAS RK

**I. K. Beisembetov**

Deputy editor in chief

**Zholtayev G.Zh.** prof., dr. geol-min. sc.

E d i t o r i a l b o a r d:

**Abakanov T.D.** prof. (Kazakhstan)  
**Abisheva Z.S.** prof., academician (Kazakhstan)  
**Agabekov V.Ye.** academician (Belarus)  
**Aliyev T.** prof., academician (Azerbaijan)  
**Bakirov A.B.** prof., (Kyrgyzstan)  
**Bespayev Kh.A.** prof. (Kazakhstan)  
**Bishimbayev V.K.** prof., academician (Kazakhstan)  
**Buktukov N.S.** prof., academician (Kazakhstan)  
**Bulat A.F.** prof., academician (Ukraine)  
**Ganiyev I.N.** prof., academician (Tadjikistan)  
**Gravis R.M.** prof. (USA)  
**Yergaliev G.K.** prof., academician (Kazakhstan)  
**Zhukov N.M.** prof. (Kazakhstan)  
**Kozhakhmetov S.M.** prof., academician (Kazakhstan)  
**Kontorovich A.Ye.** prof., academician (Russia)  
**Kurskeyev A.K.** prof., academician (Kazakhstan)  
**Kurchavov A.M.** prof., (Russia)  
**Medeu A.R.** prof., academician (Kazakhstan)  
**Muhamedzhanov M.A.** prof., corr. member. (Kazakhstan)  
**Nigmatova S.A.** prof. (Kazakhstan)  
**Ozdoyev S.M.** prof., academician (Kazakhstan)  
**Postolatii V.** prof., academician (Moldova)  
**Rakishev B.R.** prof., academician (Kazakhstan)  
**Seitov N.S.** prof., corr. member. (Kazakhstan)  
**Seitmuratova Ye.U.** prof., corr. member. (Kazakhstan)  
**Stepanets V.G.** prof., (Germany)  
**Humphery G.D.** prof. (USA)  
**Steiner M.** prof. (Germany)

**News of the National Academy of Sciences of the Republic of Kazakhstan. Series of geology and technology sciences.**

**ISSN 2518-170X (Online),**

**ISSN 2224-5278 (Print)**

Owner: RPA "National Academy of Sciences of the Republic of Kazakhstan" (Almaty)

The certificate of registration of a periodic printed publication in the Committee of information and archives of the Ministry of culture and information of the Republic of Kazakhstan N 10892-Ж, issued 30.04.2010

Periodicity: 6 times a year

Circulation: 300 copies

Editorial address: 28, Shevchenko str., of. 219, 220, Almaty, 050010, tel. 272-13-19, 272-13-18,  
<http://nauka-nanrk.kz/geology-technical.kz>

---

© National Academy of Sciences of the Republic of Kazakhstan, 2019

Editorial address: Institute of Geological Sciences named after K.I. Satpayev  
69a, Kabanbai batyr str., of. 334, Almaty, 050010, Kazakhstan, tel.: 291-59-38.

Address of printing house: ST "Aruna", 75, Muratbayev str, Almaty

NEWS

OF THE NATIONAL ACADEMY OF SCIENCES OF THE REPUBLIC OF KAZAKHSTAN

SERIES OF GEOLOGY AND TECHNICAL SCIENCES

ISSN 2224-5278

Volume 1, Number 433 (2019), 242 – 247

<https://doi.org/10.32014/2019.2518-170X.29>

UDC 539.3 (043.3)

A. Almagambetova<sup>1</sup>, S. Tileubay<sup>1</sup>, L. Taimuratova<sup>2</sup>, A. Seitmuratov<sup>1</sup>, K. Kanibaikyzy<sup>1</sup>

<sup>1</sup>The Korkyt Ata Kyzylorda state University, Kyzylorda, Kazakhstan,

<sup>2</sup>The Sh. Esenov Caspian state University of technology and engineering. Aktau, Kazakhstan.

E-mail: aldajarovna\_@mail.ru, sarsen-00@mail.ru, taimuratova@mail.ru, angisin\_@mail.ru, VIP kundyz@mail.ru

### PROBLEM ON THE DISTRIBUTION OF THE HARMONIC TYPE RELAY WAVE

**Abstract.** In this paper, we study the class of flat problems on the effect of moving loads on the surface of a laminated plate. The problems of this class are of great practical interest and in addition, can serve as a benchmark for the development of certain numerical algorithms for solving dynamic problems.

Among various periodic and non-periodic motions of deformable medium, plane waves of simple harmonic type, distributed along the surface of a body or half-plane, whose influence is limited by the vicinity of this surface, are of great importance. Therefore, we consider the problem of the distribution of the relay wave.

**Key words:** stratified plates, live-load, waves of Relay, wave equalization.

The equation of motion of a half-plane material in potentials  $\varphi$ ,  $\psi$  is described by wave equations.

$$\begin{aligned} \frac{\partial^2 \varphi}{\partial x^2} + \frac{\partial^2 \varphi}{\partial z^2} &= \frac{1}{a^2} \frac{\partial^2 \varphi}{\partial t^2}; \\ \frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial z^2} &= \frac{1}{b^2} \frac{\partial^2 \psi}{\partial t^2}, \end{aligned} \quad (1)$$

where  $a$  and  $b$  are the distribution speed of the longitudinal and transverse wave, respectively.

We assume that the boundary of the half-plane  $z=0$  is stress-free, i.e.

$$\sigma_{zz} = \sigma_{xz} = 0 \quad (z = 0) \quad (2)$$

Let there be an elastic half-plane  $z \leq 0$ .

Suppose that a flat harmonic wave propagates in the medium, i.e. potentials  $\varphi$  и  $\psi$  will be given in the form of [1]

$$\varphi(x, z, t) = \Phi_0(z) \exp[i(pt - qx)]; \quad \psi(x, z, t) = \Psi_0(z) \exp[i(pt - qx)], \quad (3)$$

$\Phi_0$  and  $\Psi_0$  satisfies the equations

$$\Phi_0'' - \left( q^2 - \frac{p^2}{a^2} \right) \Phi_0 = 0; \quad \Psi_0'' - \left( q^2 - \frac{p^2}{b^2} \right) \Psi_0 = 0. \quad (4)$$

Considering oscillations dacying with depth  $z \rightarrow -\infty$ , there must be met condition

$$q^2 - \frac{p^2}{a^2} > 0; \quad q^2 - \frac{p^2}{b^2} > 0; \quad (5)$$

But since the speeds  $a$  and  $b$  satisfy the inequality  $a > b$ , it suffices to fulfill one condition instead of conditions (5)

$$\frac{p}{q} < b \quad (6)$$

Therefore, solutions of equations (4), decayed at infinity  $z \rightarrow -\infty$ , have the form

$$\Phi_0(z) = A \exp\left(\sqrt{q^2 - \frac{p^2}{a^2}} \cdot z\right); \quad \Psi_0(z) = B \exp\left(\sqrt{q^2 - \frac{p^2}{b^2}} \cdot z\right), \quad (7)$$

and for potentials  $\varphi$  и  $\psi$  we get expressions

$$\varphi = A \exp\left[i(pt - qx) + \sqrt{q^2 - \frac{p^2}{a^2}} z\right]; \quad \psi = B \exp\left[i(pt - qx) + \sqrt{q^2 - \frac{p^2}{b^2}} z\right], \quad (8)$$

where A and B are arbitrary constants of integration.

Putting solutions (7) into the boundary conditions (2), we obtain

$$A \left[ 2 - \left(\frac{p}{qb}\right)^2 \right] + 2iB \sqrt{1 - \left(\frac{p}{qb}\right)^2} = 0; \quad -2iA \sqrt{1 - \left(\frac{p}{qa}\right)^2} + B \left[ 2 - \left(\frac{p}{qb}\right)^2 \right] = 0. \quad (9)$$

In order for the solution of the problem to be non-zero, it is necessary that the determinant of system (9) be non-zero, i.e. to make the relation [2]

$$\left[ 2 - \left(\frac{p}{qb}\right)^2 \right]^2 - 4 \sqrt{1 - \left(\frac{p}{qb}\right)^2} \sqrt{1 - \left(\frac{p}{qa}\right)^2} = 0. \quad (10)$$

The ratio  $(p/q)$  is called the propagation velocity of the relay surface wave.

Denoting  $\xi = \left(\frac{p}{qb}\right)^2$  and introducing the Poisson's ratio  $\nu$ , from relation (10) we obtain the equation

for the dimensionless velocity of the relay surface wave  $\sqrt{\xi}$ :

$$\xi^3 - 8\xi^2 + 8\xi \frac{2-\nu}{1-\nu} - 8 \frac{1}{1-\nu} = 0. \quad (11)$$

Equation (11) has a single real positive root [1, 3,4].

If through  $z_1$  и  $z_2$  and designate the depth of penetration at which the amplitude of the voltage drops in  $e$  times due to the longitudinal and transverse wave, respectively, then for them we get the expression

$$z_1 = -\frac{l}{2\pi\sqrt{1-a^{-2}b^2\xi}}; \quad z_2 = -\frac{l}{2\pi\sqrt{1-\xi}},$$

at the same time  $l = \frac{1}{q}$  - the wavelength. For example, with  $\nu = 0,5$  we have

$$z_1 = -\frac{l}{2\pi}; \quad z_2 \cong -\frac{l\sqrt{10}}{2\pi}.$$

Let the normal and tangential load intensity  $-F_1(x+Dt)$  и  $-F_2(x+Dt)$  be distributed on the surface  $z=0$  with constant speed  $D$  i.e. when  $z=0$  we have boundary conditions

$$\sigma_{zz} = -F_1(x+Dt); \quad \sigma_{xz} = -F_2(x+Dt). \quad (12)$$

Initial conditions for such a problems are absent. [2, 47-50].  
We introduce moving coordinates

$$x' = x + Dt; \quad y' = y,$$

and the strokes in the future for simplicity will be omitted. Then for potentials  $\varphi$  and  $\psi$  we get the equations

$$\alpha^2 \frac{\partial^2 \varphi}{\partial x^2} - \frac{\partial^2 \varphi}{\partial z^2} = 0;$$

$$\beta^2 \frac{\partial^2 \psi}{\partial x^2} - \frac{\partial^2 \psi}{\partial z^2} = 0;$$

$$\alpha^2 = (D/a)^2 - 1; \quad \beta^2 = (D/b)^2 - 1. \quad (13)$$

General solutions of equations (13) are d'Alembert method and have the form

$$\begin{aligned} \varphi(x, z) &= \varphi_1(x + \alpha z) + \varphi_2(x - \alpha z); \\ \psi(x, z) &= \psi_1(x + \beta z) + \psi_2(x - \beta z). \end{aligned} \quad (14)$$

By virtue of the absence of reflected waves from the lower infinitely distant boundary of the function  $\varphi_2$  and  $\psi_2$  should go to zero and for  $\varphi_1$  and  $\psi_1$  from the boundary conditions (12) we obtain the functional relations [5]

$$\begin{aligned} (\beta^2 - 1)\varphi_1''(x) - 2\beta\psi_1''(x) &= -\frac{F_1(x)}{\rho D^2}(\beta^2 + 1)H(x); \\ 2\alpha\varphi_1''(x) + (\beta^2 - 1)\psi_1''(x) &= -\frac{F_2(x)}{\rho D^2}(\beta^2 + 1)H(x). \end{aligned} \quad (15)$$

From relations (15) we get

$$\begin{aligned} \varphi_1''(x) &= \frac{\beta^2 + 1}{\rho D^2} [(\beta^2 - 1)F_1(x) + 2\beta F_2(x)]H(x)\Delta^{-1}; \\ \psi_1''(x) &= \frac{\beta^2 + 1}{\rho D^2} [2\alpha F_1(x) - (\beta^2 - 1)F_2(x)]H(x)\Delta^{-1}; \end{aligned}$$

$$\Delta = 4\alpha\beta + (\beta^2 - 1)^2. \quad (16)$$

Using dependencies (16) for stress values, we obtain the expression



$$\Delta \cdot \sigma_{xx} = -(\beta^2 - 2\alpha^2 + 1)[(\beta^2 - 1)F_1(x + \alpha z) + 2\beta F_2(x + \alpha z)] \times \\ \times H(x + \alpha z) + 2\beta [2\alpha F_1(x + \beta z) - (\beta^2 - 1)F_2(x + \beta z)]H(x + \beta z);$$

$$\Delta \cdot \sigma_{zz} = -(\beta^2 - 1)[(\beta^2 - 1)F_1(x + \alpha z) + 2\beta F_2(x + \alpha z)]H(x + \alpha z) - \\ - 2\beta [2\alpha F_1(x + \beta z) - (\beta^2 - 1)F_2(x + \beta z)]H(x + \beta z); \tag{17}$$

$$\Delta \cdot \sigma_{xz} = -2\alpha [(\beta^2 - 1)F_1(x + \alpha z) + 2\beta F_2(x + \alpha z)]H(x + \alpha z) + \\ + (\beta^2 - 1)[2\alpha F_1(x + \beta z) - (\beta^2 - 1)F_2(x + \beta z)]H(x + \beta z);$$

$$H(\zeta) = \begin{cases} 1, & \zeta \geq 0 \\ 0, & \zeta < 0 \end{cases}$$

and for shift  $u$  and  $w$  accordingly

$$u = -\frac{\beta^2 + 1}{\rho D^2 \Delta} [(\beta^2 - 1)F_3(x + \alpha z) + 2\beta F_4(x + \alpha z)]H(x + \alpha z) + \\ + \beta \frac{\beta^2 + 1}{\rho D^2 \Delta} [2\alpha F_3(x + \beta z) - (\beta^2 - 1)F_4(x + \beta z)]H(x + \beta z); \\ w = -\alpha \frac{\beta^2 + 1}{\rho D^2 \Delta} [(\beta^2 - 1)F_3(x + \alpha z) + 2\beta F_4(x + \alpha z)] \times \\ \times H(x + \alpha z) - \frac{\beta^2 + 1}{\rho D^2 \Delta} [2\alpha F_3(x + \beta z) - (\beta^2 - 1)F_4(x + \beta z)]H(x + \beta z) \tag{18}$$

where  $F_3(x) = \int_0^x F_1(\xi) d\xi$ ;  $F_4(x) = \int_0^x F_2(\xi) d\xi$ .

Let it be  $F_2 = 0$  and consider the stress  $\sigma_{xx}$  on the boundary  $z = 0$ . We obtain

$$\sigma_{xx} = F(v, D_0)F_1(x); \quad D_0 = D/a,$$

where  $F(v, D_0) = \frac{A_1(v, D_0) - A_2(v, D_0)B(v, D_0)}{A_1(v, D_0) - A_2(v, D_0)}$ ;

$$A_1 = (1 - 2v)^{3/2} \sqrt{(D_0^2 - 1)(1 - v) - (1 - 2v)};$$

$$A_2 = [D_0^2(1 - v) - (1 - 2v)];$$

$$B = [D_0^2(1 - v) - (D_0^2 - 1)(1 - 2v)]$$

Let an elastic layer  $0 \geq z > -h$   $|x| < \infty$  lie on the half-space  $z \leq -h$ , over the surface of which the normal load is distributed, i.e. when  $z = 0$  we have boundary conditions

$$\sigma_{zz}^{(0)} = -F(x + Dt); \quad \sigma_{xz}^{(0)} = 0. \tag{19}$$

The sizes and parameters of the layer will be denoted by the index "0", and the half-space - by the index "1".

At the contact boundary  $z = -h$ , you can set the conditions: hard contact

$$\sigma_{zz}^{(0)} = \sigma_{zz}^{(1)}; \quad \sigma_{xz}^{(0)} = \sigma_{xz}^{(1)}; \quad u_0 = u_1; \quad w_0 = w_1; \quad (20)$$

perfect contact

$$\sigma_{zz}^{(0)} = \sigma_{zz}^{(1)}; \quad \sigma_{xz}^{(0)} = \sigma_{xz}^{(1)} = 0; \quad w_0 = w_1; \quad (21)$$

Can be set other conditions for  $z = -h$ .

In moving coordinates, solutions of equations for potentials in a layer and a half-plane have the form [3, 171-176].

$$\alpha_j^2 \frac{\partial^2 \varphi_j}{\partial x^2} - \frac{\partial^2 \varphi_j}{\partial z^2} = 0; \quad \beta_j^2 \frac{\partial^2 \psi_j}{\partial x^2} - \frac{\partial^2 \psi_j}{\partial z^2} = 0;$$

$$\left( x' = \frac{x + Dt}{h}; \quad y' = \frac{y}{h}; \quad \varphi_0 = \frac{\varphi_0}{h^2}; \quad \psi_0 = \frac{\psi_0}{h^2} \right). \quad (22)$$

Putting (22) into the boundary conditions (20), we obtain a system of functional equations which using in expressions for displacements  $u_j, w_j$  and stresses  $\sigma_{ij}$ , we obtain the solution of the problem.

**А. А. Алмағамбетова<sup>1</sup>, С. Ш. Тілеубай<sup>1</sup>, Л. У. Таймуратова<sup>2</sup>,  
А. Ж. Сейтмұратов<sup>1</sup>, Қ. Қанибайқызы<sup>1</sup>**

<sup>1</sup>Қорқыт Ата атындағы Қызылорда мемлекеттік университеті, Қызылорда, Қазақстан,

<sup>2</sup>Ш. Есенов атындағы Каспий мемлекеттік технология және инжиниринг университеті, Ақтау, Қазақстан

### ГАРМОНИКАЛЫҚ ТИПТЕГІ РЕЛЕЙ ТОЛҚЫНДАРЫНЫҢ ТАРАЛУЫ ЖАЙЛЫ ЕСЕП

**Аннотация.** Жұмыста қатпарлы пластинкалардың бетіне қозғалмалы жүктемелердің әсері туралы бірнеше жазық есептер класы зеріттеледі. Осы типтес динамикалық есептер проблемалары жайлы смәселелерді шешуге арналған белгілі сандық алгоритмдерді дамытудың негізгі бағыты бола алуымен қызығушылық тудырады. Деформацияланатын ортаның әртүрлі периодты және преиодтты емес қозғалыстарының арасында шектелген дененің бетіне немесе жарты жазықтыққа тарайтын қарапайым гармоникалық үлгідегі жазық толқындар әсер етеді. Сондықтан да Релей толқынының таралуын зерттейтін боламыз.

**Түйін сөздер:** қатпарлы пластинкалар, қозғалмалы жүктеме, Релей толқындары, толқындар теңлеуі.

**А. А. Алмағамбетова<sup>1</sup>, С. Ш. Тілеубай<sup>1</sup>, Л. У. Таймуратова<sup>2</sup>,  
А. Ж. Сейтмұратов<sup>1</sup>, Қ. Қанибайқызы<sup>1</sup>**

<sup>1</sup>Қызылординский государственный университет им. Коркыт Ата, Кызылорда, Казахстан,

<sup>2</sup>Каспийский государственный университет технологий и инжиниринга им. Ш. Есенова, Ақтау, Казахстан

### ЗАДАЧА О РАСПРОСТРАНЕНИИ ВОЛНЫ РЕЛЕЯ ГАРМОНИЧЕСКОГО ТИПА

**Аннотация.** В работе исследуем класс плоских задач о воздействии подвижных нагрузок на поверхность слоистой пластинки. Задачи данного класса представляют большой прикладной интерес и, кроме того, могут служить эталоном для разработки тех или иных численных алгоритмов для решения динамических задач. Среди различных периодических и непериодических движений деформируемых сред важное значение имеют плоские волны простого гармонического типа, распространяющиеся по поверхности тела или полуплоскости, влияние которых ограничивается окрестностью этой поверхности. Поэтому рассмотрим задачу о распространении волны Релея.

**Ключевые слова:** слоистые пластинки, подвижная нагрузка, волны Релея, волновые уравнение.

**Information about authors:**

Almagambetova Aigul Aldajarovna, Candidate of pedagogical sciences, Senior Lecturer The Korkyt Ata Kyzylorda State University, Kyzylorda, Kazakhstan; aldajarovna\_@mail.ru; <https://orcid.org/0000-0002-8790-8948>

Tileubay Sarsenkul Shaykamalqız, Candidate of pedagogical sciences, The Korkyt Ata Kyzylorda State University, Kyzylorda, Kazakhstan; sarsen-00@mail.ru; <https://orcid.org/0000-0001-6590-2097>

Taimuratova Lidiya Ungarbaevna, Candidate of physical and mathematical sciences. Associate Professor of «Natural Sciences» Caspian state University of technology and engineering named after Sh. Esenov, Aktau, Kazakhstan; taimuratova@mail.ru; <https://orcid.org/0000-0002-1692-4350>

Seitmuratov Angisin, Doktor of Physical and Matematical Sciences, Professoz, The Korkyt Ata Kyzylorda State University, Kyzylorda, Kazakhstan; angisin\_@mail.ru; <https://orcid.org/0000-0002-9622-9584>

Kanibaikyzy Kundyzyay, Master degree of pedagogical sciences, The Korkyt Ata Kyzylorda State University, Kyzylorda, Kazakhstan; VIP kundyzyay@mail.ru; <https://orcid.org/0000-0002-3713-1608>

**REFERENCES**

[1] Filippov I.G., Filippov S.I. Dynamic stability theory of rods. Proceedings of the Russian-Polish seminar. Theoretical Foundations of construction. Warsaw, 1995. P. 63-69.

[2] Filippov I.G. An approximate method for solving dynamic viscoelastic media // PMM. 1979. 43(1). P. 133-137.

[3] Filippov I.G., Filippov S.I., Kostin V.I. Dynamics of two-dimensional composites // Proceedings of the International Conference on Mechanics and Materials, USA, Los Angeles, 1995. P. 75-79.

[4] Seitmuratov A., Medeubaev N., Yeshmurat G., Kudebayeva G. (2018) Approximate solution of the an elastic layer vibration task being exposed of moving load // News of the national academy of sciences of the Republic of Kazakhstan. Series physic-mathematical. 2 (318). P. 54-60 (in Eng.).

[5] Seitmuratov A.Z., Nurlanova BM., Medeubaev N. Equations of vibration of a two-dimensionally layered plate strictly based on the decision of various boundaty-value problems // Bulletin of the Karaganda university-mathematics. 2017. 3(87). P. 109-116 (in Eng.).

[6] Seitmuratov A., Yergalauova Z., Makhambayeva, Bexeitova A. Axismetric problems of elastic layer oscillation limited by rigid or deformed boundries // News of the national academy of sciences of the Republic of Kazakhstan. Series of geology and technical sciences. 2018. 1. P. 127-135 (in Eng.).

[7] Ashirbayev N., Ashirbayeva Zh., Sultanbek T., Shomanbayeva M. Waves of elastic stresses in the doublyconnected domain // Vestnik KarGU. Cerija matematika. 2018. 2(90). P. 18-25.

[8] Seytmuratov A.Z., Zharylgapova D.M., Medeubaev N.K., Ibraeva A.A. Applied tasks of plates fluctuation under more difficult boundary conditions // News of the National Academy of Sciences of the Republic of Kazakhstan. Series of Geology and Technical Sciences. 2017. 3(423). P. 228-236 (in Eng.).

[9] Ashirbayev N.K., Banas J., Dubiel A. Solvability of an Integral Equation of Volterra-Wiener-Hopf Type // Abstract and Applied Analysis. Vol. 2014 (2014). Article ID 982079. 9 p. DOI 10.1155/2014/982079.

[10] Seitmuratov A., Ramazanov M., Medeubaev N., Kaliev B. Mathematical theory of vibration of elastic or viscoelastic plates, under non-stationary external influences // News of the National Academy of Sciences of the Republic of Kazakhstan. Series of Geology and Technical Sciences. 2017. 4(320). P. 5-14. (in Eng.). <https://doi.org/10.32014/2018.2518-170X>; ISSN 2518-170X (Online), ISSN 2224-5278 (Print).

[11] Seitmuratov A., Seylova Z.T., Kanibaikyzy K., Smakhanova A.K., Serikbol S.M. Approximate equation plate oscillation for transverse displacement of points of the median plane // News of the National Academy of Sciences of the Republic of Kazakhstan. Series of Geology and Technical Sciences. 2018. 3(429). P. 258-266. (in Eng.). <https://doi.org/10.32014/2018.2518-170X>; ISSN 2518-170X (Online), ISSN 2224-5278 (Print).

---

**Publication Ethics and Publication Malpractice  
in the journals of the National Academy of Sciences of the Republic of Kazakhstan**

For information on Ethics in publishing and Ethical guidelines for journal publication see <http://www.elsevier.com/publishingethics> and <http://www.elsevier.com/journal-authors/ethics>.

Submission of an article to the National Academy of Sciences of the Republic of Kazakhstan implies that the described work has not been published previously (except in the form of an abstract or as part of a published lecture or academic thesis or as an electronic preprint, see <http://www.elsevier.com/postingpolicy>), that it is not under consideration for publication elsewhere, that its publication is approved by all authors and tacitly or explicitly by the responsible authorities where the work was carried out, and that, if accepted, it will not be published elsewhere in the same form, in English or in any other language, including electronically without the written consent of the copyright-holder. In particular, translations into English of papers already published in another language are not accepted.

No other forms of scientific misconduct are allowed, such as plagiarism, falsification, fraudulent data, incorrect interpretation of other works, incorrect citations, etc. The National Academy of Sciences of the Republic of Kazakhstan follows the Code of Conduct of the Committee on Publication Ethics (COPE), and follows the COPE Flowcharts for Resolving Cases of Suspected Misconduct ([http://publicationethics.org/files/u2/New\\_Code.pdf](http://publicationethics.org/files/u2/New_Code.pdf)). To verify originality, your article may be checked by the Cross Check originality detection service <http://www.elsevier.com/editors/plagdetect>.

The authors are obliged to participate in peer review process and be ready to provide corrections, clarifications, retractions and apologies when needed. All authors of a paper should have significantly contributed to the research.

The reviewers should provide objective judgments and should point out relevant published works which are not yet cited. Reviewed articles should be treated confidentially. The reviewers will be chosen in such a way that there is no conflict of interests with respect to the research, the authors and/or the research funders.

The editors have complete responsibility and authority to reject or accept a paper, and they will only accept a paper when reasonably certain. They will preserve anonymity of reviewers and promote publication of corrections, clarifications, retractions and apologies when needed. The acceptance of a paper automatically implies the copyright transfer to the National Academy of Sciences of the Republic of Kazakhstan.

The Editorial Board of the National Academy of Sciences of the Republic of Kazakhstan will monitor and safeguard publishing ethics.

Правила оформления статьи для публикации в журнале смотреть на сайте:

[www:nauka-nanrk.kz](http://www.nauka-nanrk.kz)

**ISSN 2518-170X (Online), ISSN 2224-5278 (Print)**

<http://www.geolog-technical.kz/index.php/en/>

Верстка Д. Н. Калкабековой

Подписано в печать 06.02.2019.

Формат 70x881/8. Бумага офсетная. Печать – ризограф.

16,7 п.л. Тираж 300. Заказ 1.